

# **On Lindenmayer Systems and Autoencoders**

*Andrej Lúčny*

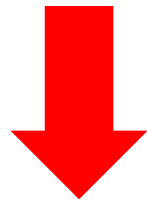
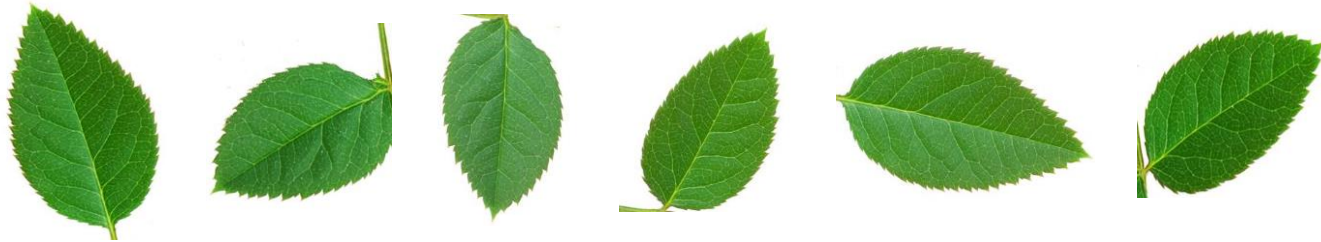
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*Comenius University, Bratislava, Slovakia*

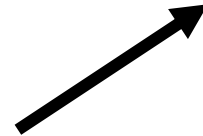
**lucny@fmph.uniba.sk**

**[http://dai.fmph.uniba.sk/w/Andrej\\_Lucny](http://dai.fmph.uniba.sk/w/Andrej_Lucny)**

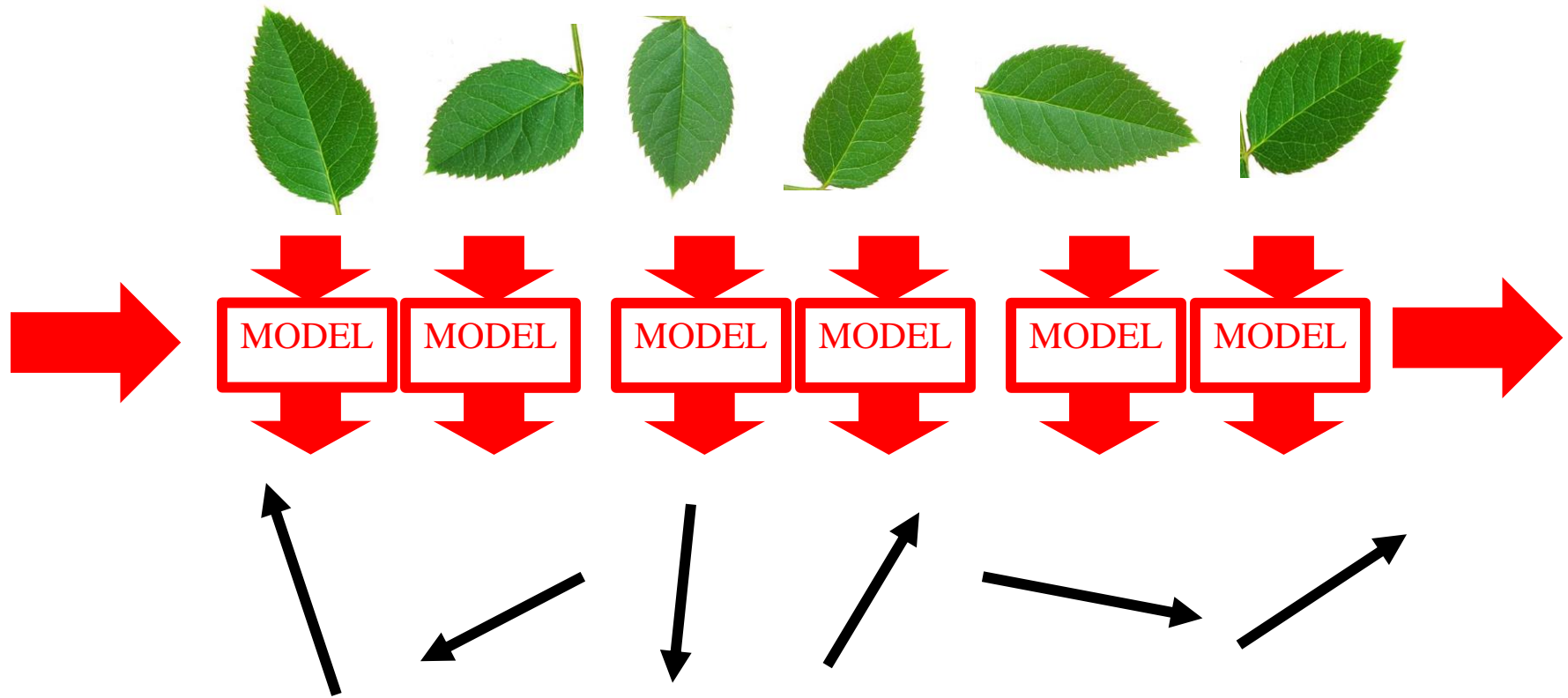
# Dataset



**ANOTATION**

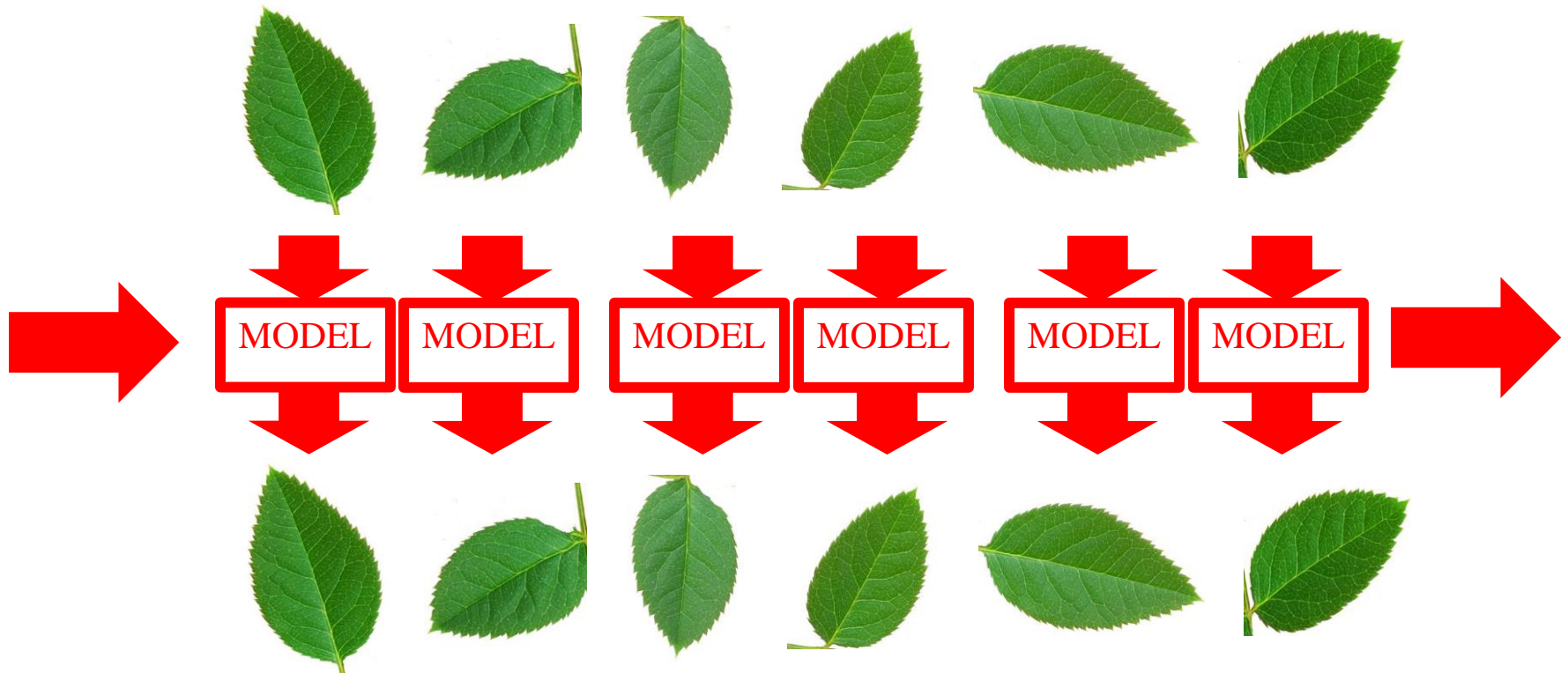


# Deep learning



**TRAINING** in a loop: from the difference between actual and wished outputs, we derive how to modify the model weights to decrease it

# Autoencoder

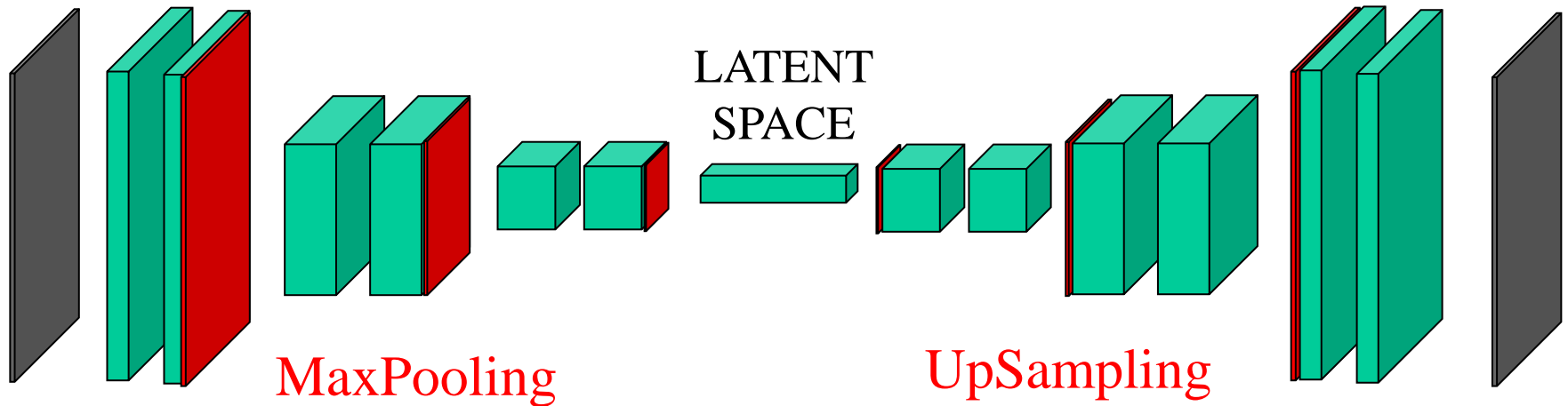


We wish to get on output the same images as on input.  
Is it useful for something? Oh, yes, it is.

# Autoencoder architecture

INPUT

OUTPUT

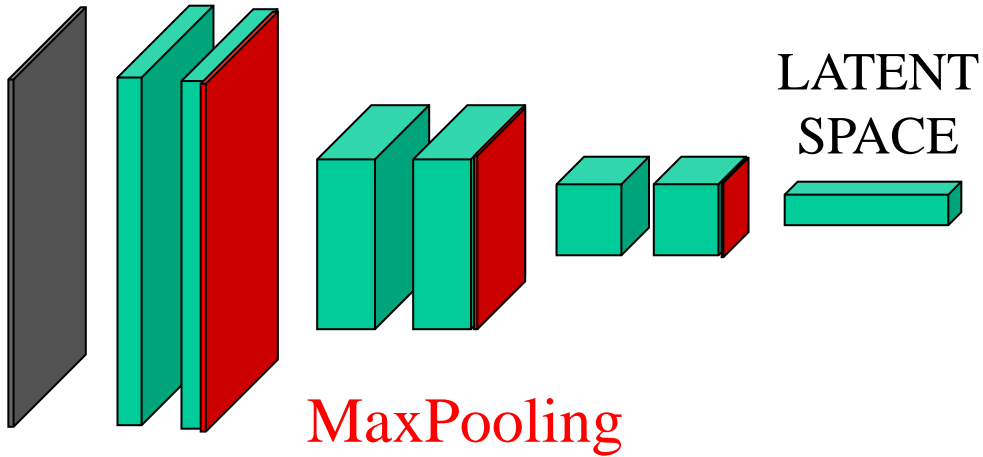


convolutional layers

If we successfully train the autoencoder, the feature vectors in the latent space have to contain the same information images from the dataset. We can split the network into encoder and decoder now.

# Encoder

INPUT



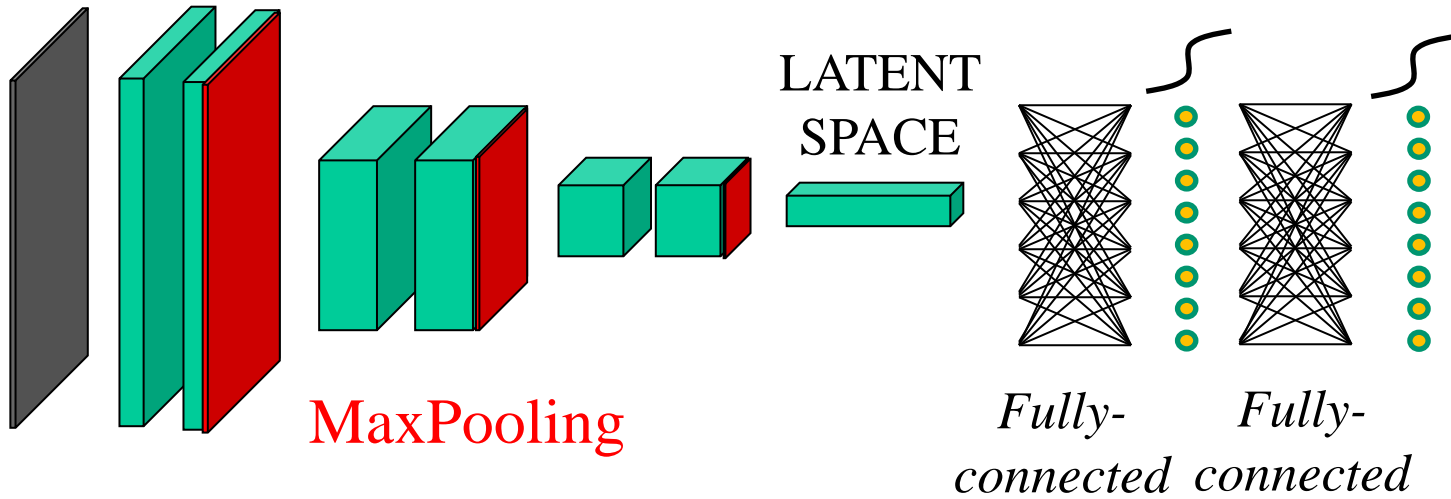
convolutional layers



$(0.1, 0.2, \dots, 0.9)$

# Regressor

INPUT



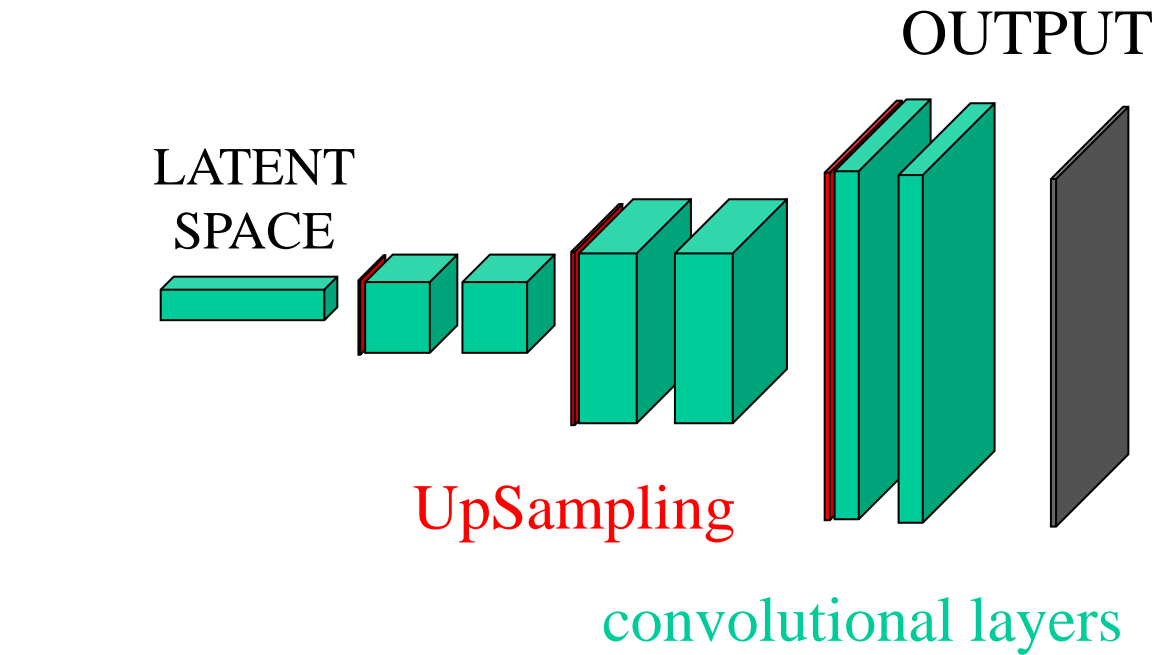
convolutional layers



$(0.1, 0.2, \dots, 0.9)$



# Decoder

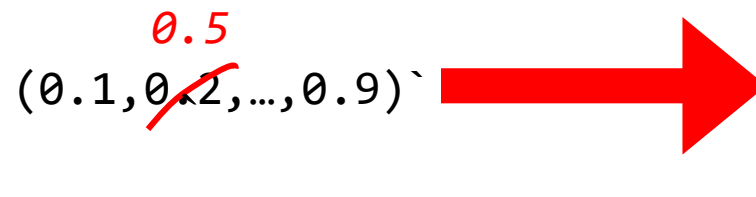
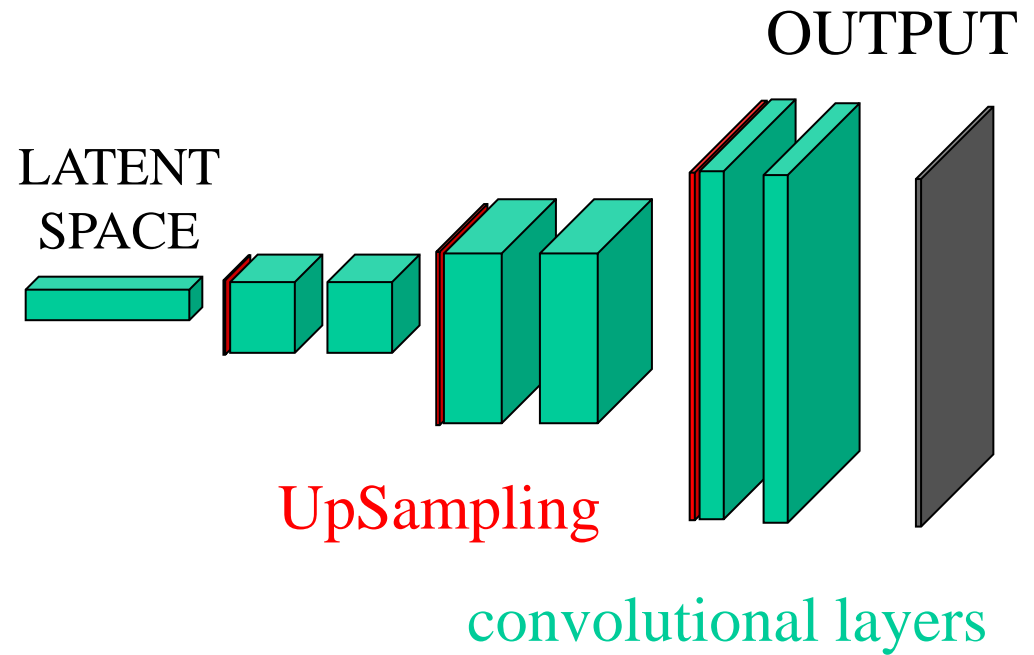


$(0.1, 0.2, \dots, 0.9)$

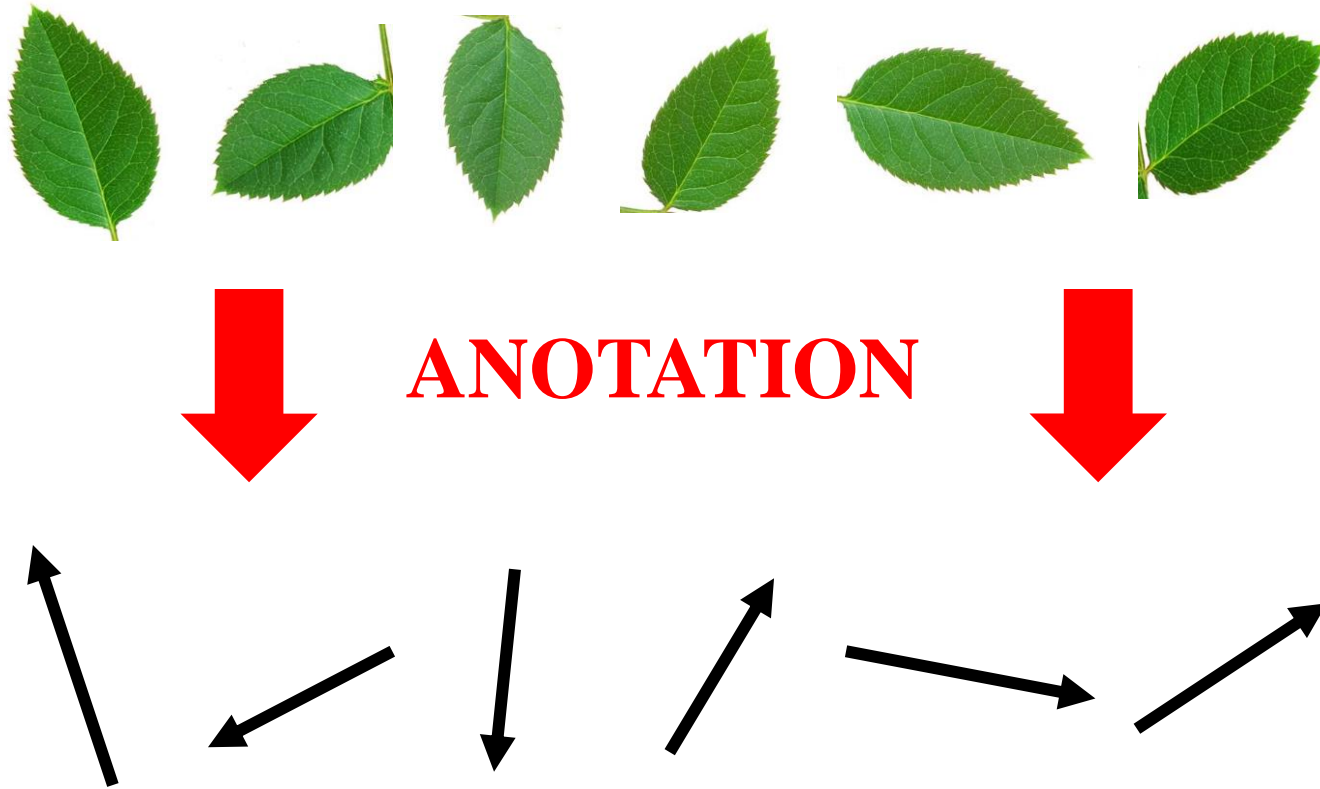




# Generator

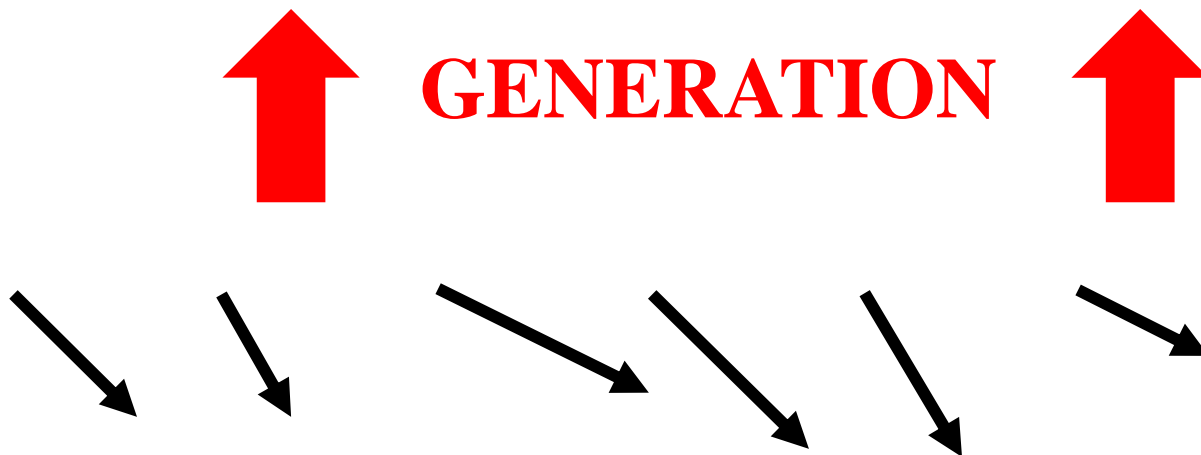
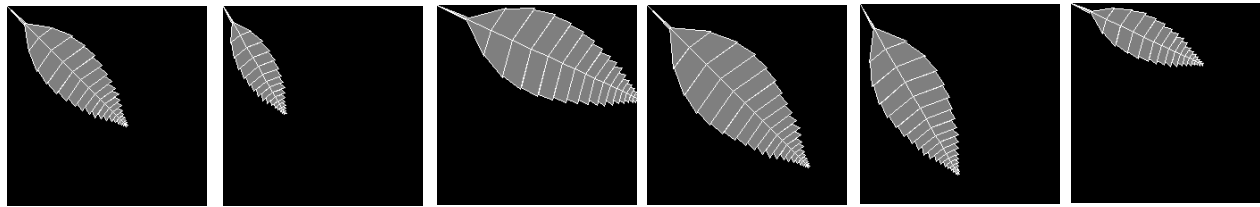


# Datasets have many parameters



Annotations do not fully describe the images

Generated datasets have a very exact  
and low number of parameters



Annotations do fully describe the images

# Parametric Lindenmayer systems

- can generate image datasets from a few parameters

---

$\omega_0$	:	$[\{A(0, 0).\}] [\{A(0, 1).\}]$
$p1$	:	$A(t, d) : d = 0 \rightarrow .G(LA, RA).$ $[+B(t)G(LC, RC, t).\] [+B(t)\{.\}A(t + 1, d)$
$p2$	:	$A(t, d) : d = 1 \rightarrow .G(LA, RA).$ $[-B(t)G(LC, RC, t).\] [-B(t)\{.\}A(t + 1, d) $
$p3$	:	$B(t) : t > 0 \rightarrow G(LB, RB)B(t - 1)$
$p4$	:	$G(s, r) \rightarrow G(s * r, r)$
$p5$	:	$G(s, r, t) : t > 1 \rightarrow G(s * r, r, t - 1)$

---

rose leaves [*Prusinkiewicz, Lindenmayer 1990*]

$$[\{A(0,0).\}][\{A(0,1).\}]$$

$$[\{.G(5,1.15).[+B(0)G(3,1.19,0).\}][+B(0)\{.]A(1,0).\}][\{.G(5,1.15).[-B(0)G(3,1.19,0).\}][+B(0)\{.]A(1,1).\}]$$

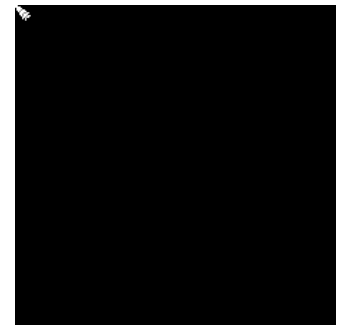
$$[\{.G(5.75,1.15).[+B(0)G(3,1.19,0).\}][+B(0)\{.].G(5,1.15).[+B(1)G(3,1.19,1).\}][+B(1)\{.]A(2,0).\}][\{.G(5.75,1.15).[-B(0)G(3,1.19,0).\}][+B(0)\{.].G(5,1.15).[-B(1)G(3,1.19,1).\}][+B(1)\{.]A(2,1).\}]$$

$$[\{.G(6.6125,1.15).[+B(0)G(3,1.19,0).\}][+B(0)\{.].G(5.75,1.15).[+G(1.3,1.25)B(0)G(3,1.19,1).\}][+G(1.3,1.25)B(0)\{.].G(5,1.15).[+B(2)G(3,1.19,2).\}][+B(2)\{.]A(3,0).\}][\{.G(6.6125,1.15).[-B(0)G(3,1.19,0).\}][+B(0)\{.].G(5.75,1.15).[-G(1.3,1.25)B(0)G ...$$


*iteration 1*

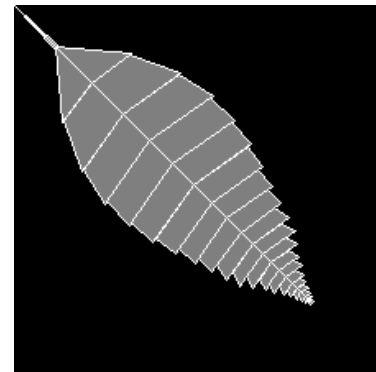


*iteration 2*



*iteration 3*

[+G(3.173828125,1.25)G(2.5390625,1.25)G(2.  
 .03125,1.25)G(1.625,1.25)G(1.3,1.25)B(8)G  
 (7.1590609796999998,1.19,8).}] [+G(3.173  
 828125,1.25)G(2.5390625,1.25)G(2.03125,1.  
 25)G(1.625,1.25)G(1.3,1.25)B(8){.}.G(8.74  
 50312499999998,1.15). [+G(2.5390625,1.25  
 )G(2.03125,1.25)G(1.625,1.25)G(1.3,1.25)B  
 (10)G(6.0160176299999999,1.19,10).}] [+G(2.  
 5390625,1.25)G(2.03125,1.25)G(1.625,1.  
 25)G(1.3,1.25)B(10){.}.G(7.604374999999999  
 9,1.15). [+G(2.03125,1.25)G(1.625,1.25)G(1  
 .3,1.25)B(12)G(5.0554769999999999,1.19,  
 12).}] [+G(2.03125,1.25)G(1.625,1.25)G(1.3  
 ,1.25)B(12){.}.G(6.6125,1.15). [+G(1.625,1  
 .25)G(1.3,1.25)B(14)G(4.248299999999999  
 95,1.19,14).}] [+G(1.625,1.25)G(1.3,1.25)B  
 (14){.}.G(5.75,1.15). [+G(1.3,1.25)B(16)G(  
 3.57,1.19,16).}] [+G(1.3,1.25)B(16){.}. ...



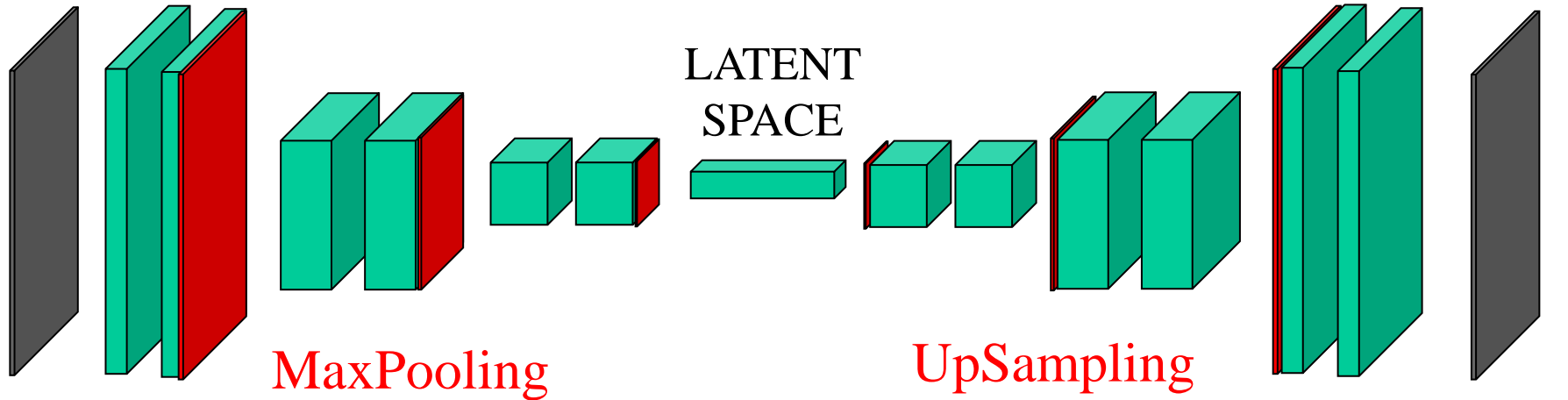
*iteration 19*

# We have investigated:

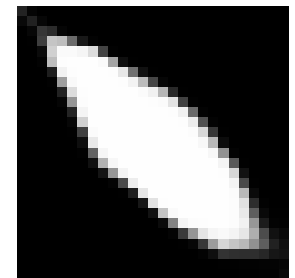
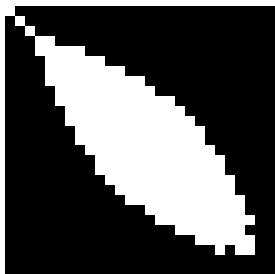
1. Can we find the parameters of the Lindenmayer system somewhere inside the latent space of the neural network that is processing a dataset produced by the Lindenmayer system?
2. Can we create a neural network that generates the same images as the Lindenmayer system?
3. And could a neural network make the images from the parameters of the Lindenmayer system?

# We have trained autoencoder

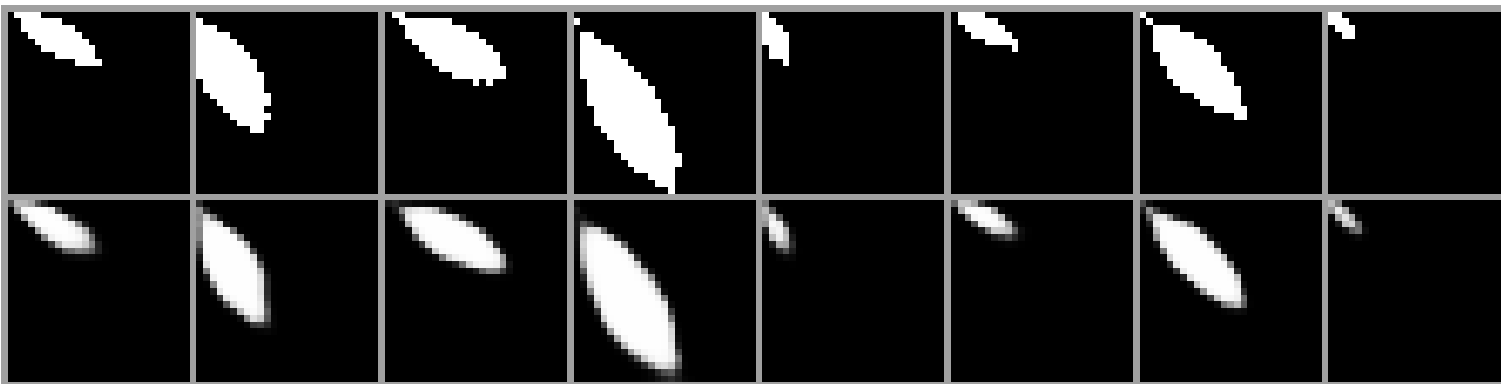
INPUT



convolutional layers

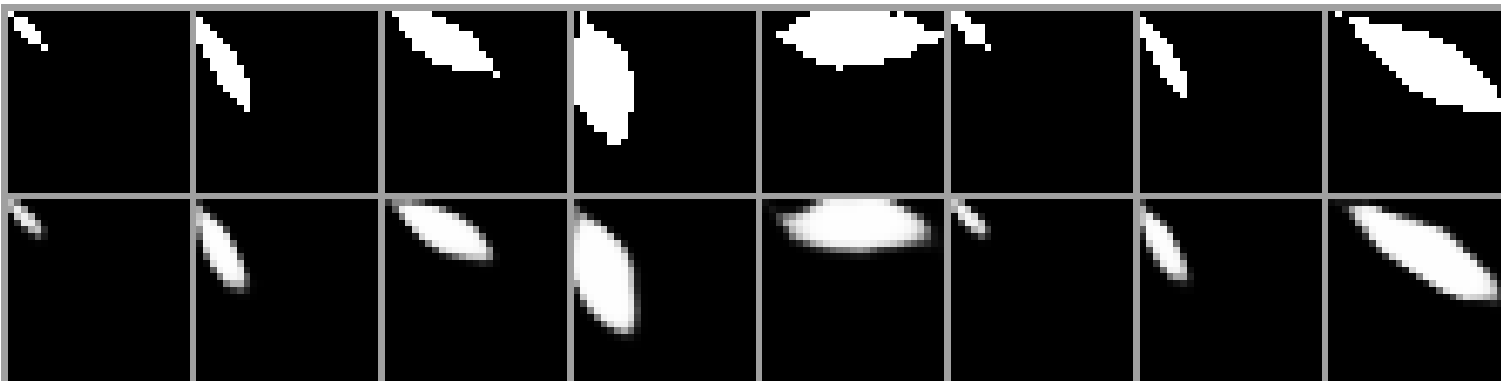






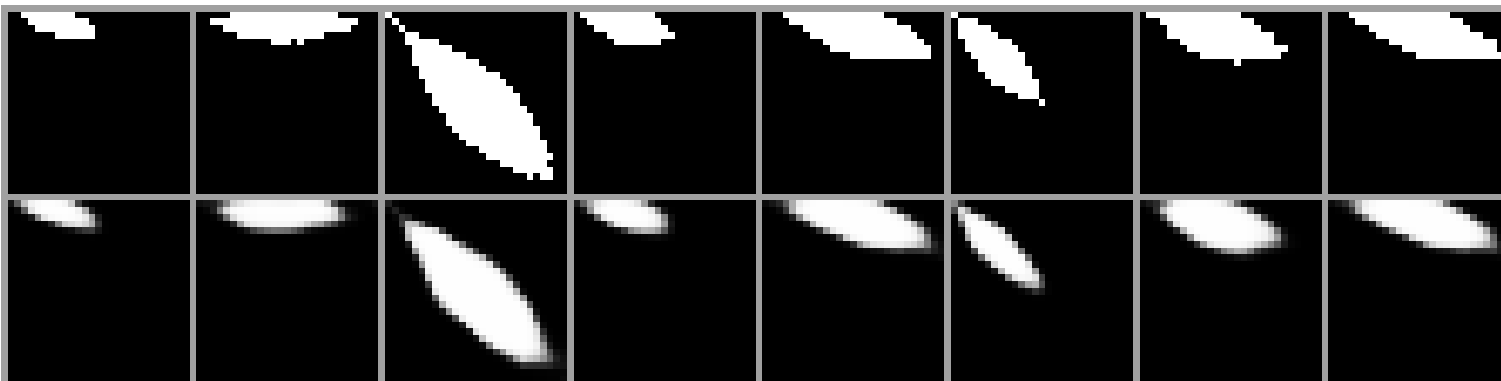
inputs

outputs



inputs

outputs



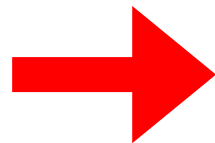
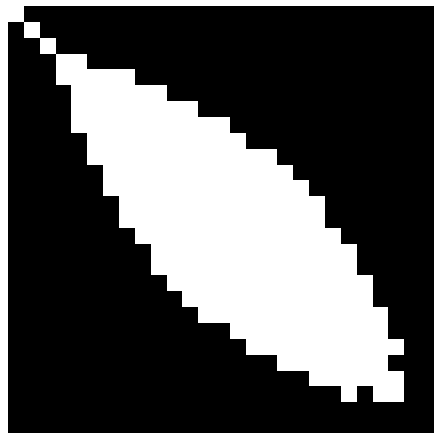
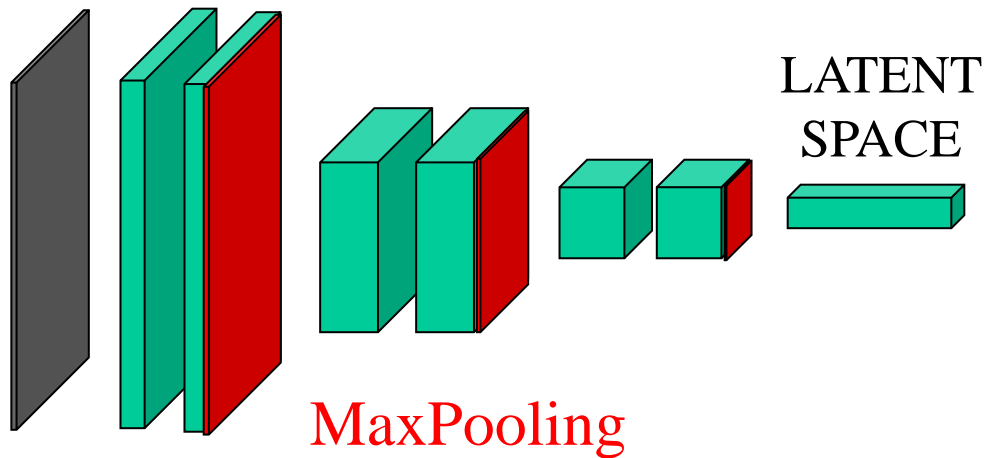
inputs

outputs

test accuracy 98,6%

Can we find the parameters of the Lindenmayer system somewhere inside the latent space of the neural network that is processing a dataset produced by the Lindenmayer system?

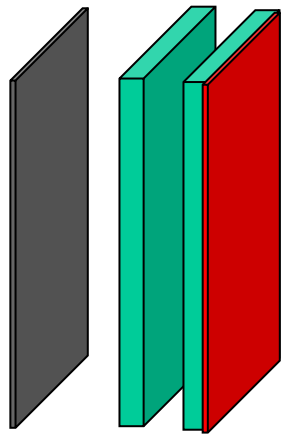
INPUT



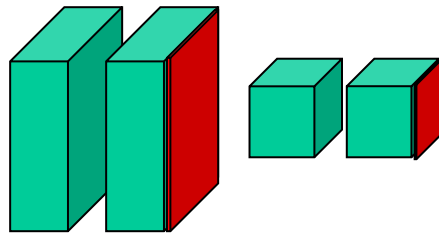
$(0.1, 0.2, \dots, 0.9)$

Can we find the parameters of the Lindenmayer system somewhere inside the latent space of the neural network that is processing a dataset produced by the Lindenmayer system?

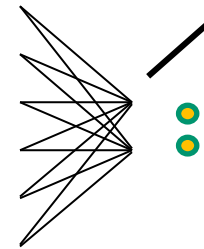
INPUT



MaxPooling  
convolutional layers



LATENT  
SPACE



*parameters of LS*

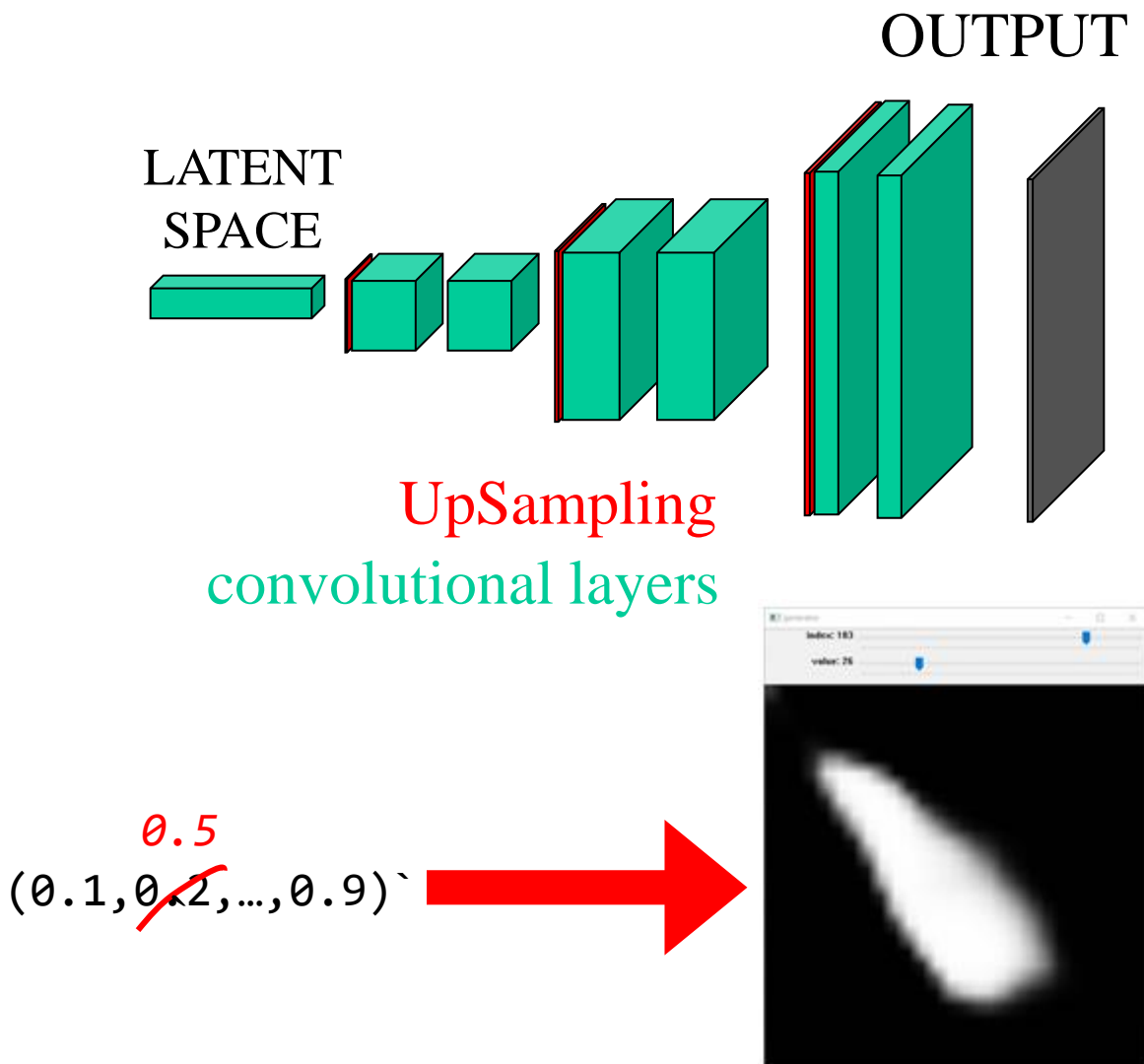
*Linear regression* is sufficient to reveal some parameters of LS



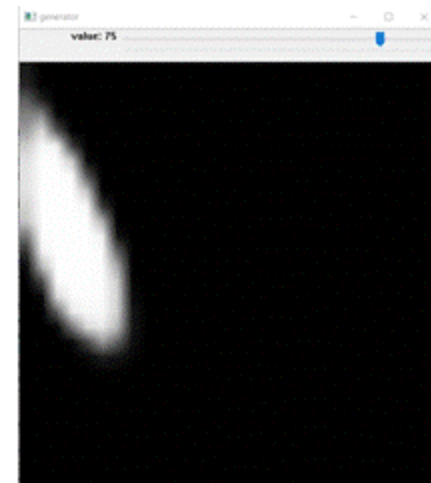
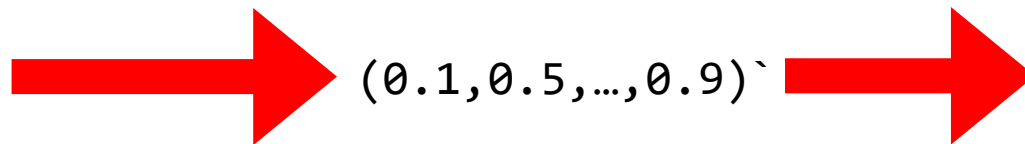
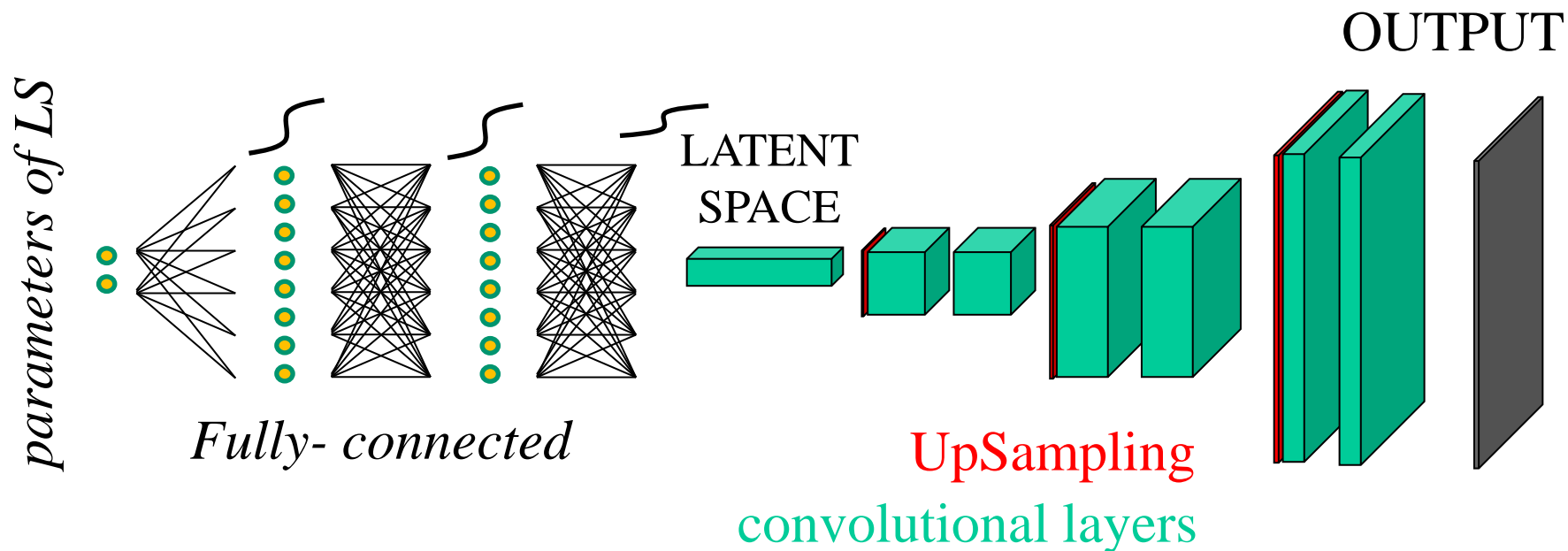
$(0.1, 0.2, \dots, 0.9)$



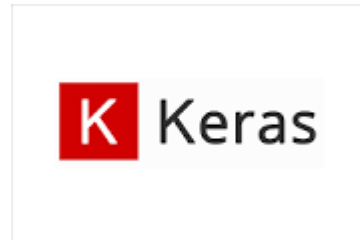
Can we create a neural network that generates the same images as the Lindenmayer system?



And could a neural network make the images from the parameters of the Lindenmayer system?



# Implementation details



[https://github.com/andy1ucny/  
On-Lindenmayer-Systems-and-Autoencoders.git](https://github.com/andy1ucny/On-Lindenmayer-Systems-and-Autoencoders.git)

# Further development

- Autoencoder architecture for higher image resolution
- Not only binary images
- Reduction of the latent space dimension
- Further investigation and better visualization of the latent space
- A simpler network for generation from parameters

Thank you!

# On Lindenmayer Systems and Autoencoders

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`https://github.com/andylucny/On-Lindenmayer-Systems-and-Autoencoders.git`